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3.

$$f(x) = (3x - 2)(x - k) - 8$$

where  $k$  is a constant.

(a) Write down the value of  $f(k)$ .

(1)

When  $f(x)$  is divided by  $(x - 2)$  the remainder is 4

(b) Find the value of  $k$ .

(2)

(c) Factorise  $f(x)$  completely.

(3)

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4. (a) Complete the table below, giving values of  $\sqrt{2^x + 1}$  to 3 decimal places.

$x$	0	0.5	1	1.5	2	2.5	3
$\sqrt{2^x + 1}$	1.414	1.554	1.732	1.957			3

(2)

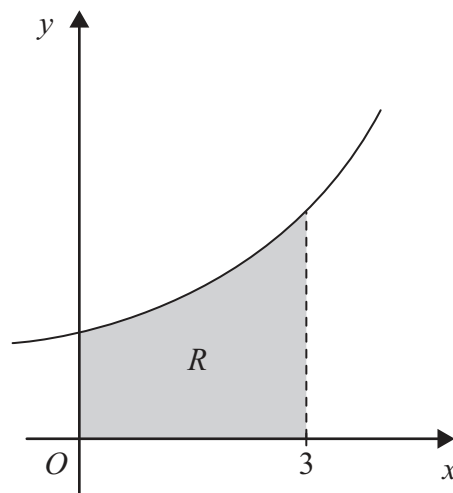


Figure 1

Figure 1 shows the region  $R$  which is bounded by the curve with equation  $y = \sqrt{2^x + 1}$ , the  $x$ -axis and the lines  $x = 0$  and  $x = 3$

(b) Use the trapezium rule, with all the values from your table, to find an approximation for the area of  $R$ .

(4)

(c) By reference to the curve in Figure 1 state, giving a reason, whether your approximation in part (b) is an overestimate or an underestimate for the area of  $R$ .

(2)

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6. The circle  $C$  has equation

$$x^2 + y^2 - 6x + 4y = 12$$

(a) Find the centre and the radius of  $C$ . **(5)**

The point  $P(-1, 1)$  and the point  $Q(7, -5)$  both lie on  $C$ .

(b) Show that  $PQ$  is a diameter of  $C$ . **(2)**

The point  $R$  lies on the positive  $y$ -axis and the angle  $PRQ = 90^\circ$ .

(c) Find the coordinates of  $R$ . **(4)**

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8. (a) Find the value of  $y$  such that

$$\log_2 y = -3$$

(2)

(b) Find the values of  $x$  such that

$$\frac{\log_2 32 + \log_2 16}{\log_2 x} = \log_2 x$$

(5)

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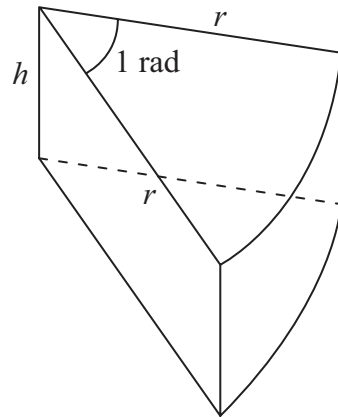


Figure 2

Figure 2 shows a closed box used by a shop for packing pieces of cake. The box is a right prism of height  $h$  cm. The cross section is a sector of a circle. The sector has radius  $r$  cm and angle 1 radian.

The volume of the box is  $300 \text{ cm}^3$ .

(a) Show that the surface area of the box,  $S \text{ cm}^2$ , is given by

$$S = r^2 + \frac{1800}{r} \quad (5)$$

(b) Use calculus to find the value of  $r$  for which  $S$  is stationary. (4)

(c) Prove that this value of  $r$  gives a minimum value of  $S$ . (2)

(d) Find, to the nearest  $\text{cm}^2$ , this minimum value of  $S$ . (2)

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